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Amendments to the Specification:

Please amend the paragraph beginning on page 15, line 5 as follows:

Although not wishing to be bound by theory, the equivalence of the methodology of the present invention with the Black-Scholes method in instances in which the assumptions upon which the Black-Scholes formula are met may be proved mathematically. In this regard, the valuation of a contingent claim determined according to the present invention can be represented as:

$$E[\max(s_T e^{-\mu T} - x e^{-rT}), 0] = \int_{-x e^{-rT}}^{\infty} (s_T e^{-\mu T} - x e^{-rT}) g(y) dy$$
 (1)

$$\underline{E[\max(s_T e^{-\mu T} - x e^{-rT}, 0)]} = \int_{-x e^{-rT}}^{\infty} (s_T e^{-\mu T} - x e^{-rT}) g(y) dy$$
 (1)

wherein s_T is the random value of the underlying asset at time T, μ is first discount rate, T is the time until the contingent claim may be exercised, x is the contingent future investment, r is the second discount rate, y equals $s_T e^{-\mu T}$, and g(y) is the probability density of y. Equation (1) can then be translated into a form more similar to the Black-Scholes formula by the following substitutions:

$$E[\max(s_T e^{-\mu T} - x e^{-rT}), 0] = \int_{-x e^{-rT}}^{\infty} (s_T e^{-\mu T} - x e^{-rT}) g(y) dy$$

$$\underline{E[\max(s_T e^{-\mu T} - x e^{-rT}, 0)]} = \int_{-x e^{-rT}}^{\infty} (s_T e^{-\mu T} - x e^{-rT}) g(y) dy$$

$$= E(s_T e^{-\mu T}) N_{d_1} - x e^{-rT} N_{d_2} = S_0 N_{d_1} - x e^{-rT} N_{d_2}$$
(2)

wherein

$$d_1 = \frac{\ln(S_0 / xe^{-rT}) + s^2 / 2}{s} \tag{3}$$

$$d_2 = \frac{\ln(S_0 / xe^{-rT}) - s^2 / 2}{s} \tag{4}$$

 $d_2 = \frac{\ln(S_0 / xe^{-rT}) - s^2 / 2}{s}$ s = std dev of $\ln(s_T e^{-\mu T})$ (5)

and wherein S₀ equals $E(s_T e^{-\mu T})$.



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In addition, it is known that:

$$\ln\left(\frac{s_T}{s_0}\right) \sim \phi \left[\left(\mu - \frac{\sigma^2}{2}\right)T, \sigma\sqrt{T}\right]$$
 (6)

$$\therefore \ln s_T \sim \phi \left[\ln s_0 + \left(\mu - \frac{\sigma^2}{2} \right) T, \sigma \sqrt{T} \right]$$
 (7)

$$\therefore \ln\left(s_T e^{-\mu T}\right) \sim \phi \left[-\mu T + \ln s_0 + \left(\mu - \frac{\sigma^2}{2}\right)T, \sigma\sqrt{T}\right]$$
 (8)

wherein ϕ denotes a normal distribution and σ is the volatility parameter utilized in the Black-Scholes method. As such, the definition of s provided by equation (4) is therefore equal to $\sigma\sqrt{T}$. By substituting this definition of s into equations (3) and (4), d_1 and d_2 may be rewritten as follows:

$$d_{1} = \frac{\ln\left(\frac{s_{0}}{x}\right) + \left(r + \frac{\sigma^{2}}{2}\right)T}{\sigma\sqrt{T}}$$

$$d_{2} = \frac{\ln\left(\frac{s_{0}}{x}\right) - \left(r + \frac{\sigma^{2}}{2}\right)T}{\sigma\sqrt{T}}$$

As described above equations (2), (3) and (4) collectively represent the Black-Scholes formula, thereby proving mathematically the equivalence of the methodology with the Black-Scholes formula in instances in which the assumptions upon which the Black-Scholes formula are based are met.

